## Further Algebra – 2021/20 GCE AS Pure Further Mathematics A

1. Nov/2021/Paper\_Y531/01/No.2

The equation  $2x^3 + 3x^2 - 2x + 5 = 0$  has roots  $\alpha$ ,  $\beta$  and  $\gamma$ .

Use a substitution to find a cubic equation with integer coefficients whose roots are  $\alpha + 1$ ,  $\beta + 1$  and  $\gamma + 1$ . [4]

[6]

#### 2. Nov/2021/Paper\_Y531/01/No.3

## In this question you must show detailed reasoning.

The equation  $x^4 - 7x^3 - 2x^2 + 218x - 1428 = 0$  has a root 3 - 5i.

Find the other three roots of this equation.

#### 3. Nov/2020/Paper\_Y531/01/No.5

# In this question you must show detailed reasoning.

The cubic equation  $5x^3 + 3x^2 - 4x + 7 = 0$  has roots  $\alpha$ ,  $\beta$  and  $\gamma$ .

Find a cubic equation with integer coefficients whose roots are  $\alpha + \beta$ ,  $\beta + \gamma$  and  $\gamma + \alpha$ . [7]