Statistical distribution – 2021/20 GCE Statistics Mathematics A

1. Nov/2021/Paper H240/02/No.14

The probability distribution of a random variable X is modelled as follows.

$$P(X = x) = \begin{cases} \frac{k}{x} & x = 1, 2, 3, 4, \\ 0 & \text{otherwise,} \end{cases}$$

where k is a constant.

(a) Show that
$$k = \frac{12}{25}$$
. [2]

- (b) Show in a table the values of X and their probabilities. [1]
- (c) The values of three independent observations of X are denoted by X_1 , X_2 and X_3 .

Find
$$P(X_1 > X_2 + X_3)$$
. [3]

In a game, a player notes the values of successive independent observations of X and keeps a running total. The aim of the game is to reach a total of exactly 7.

(d) Determine the probability that a total of exactly 7 is first reached on the 5th observation. [5]

2. Nov/2020/Paper H240/02/No.11

As part of a research project, the masses, m grams, of a random sample of 1000 pebbles from a certain beach were recorded. The results are summarised in the table.

Mass (g)	50 ≤ <i>m</i> < 150	150 ≤ <i>m</i> < 200	200 ≤ <i>m</i> < 250	250 ≤ <i>m</i> < 350
Frequency	162	318	355	165

(a) Calculate estimates of the mean and standard deviation of these masses.

The masses, x grams, of a random sample of 1000 pebbles on a different beach were also found. It was proposed that the distribution of these masses should be modelled by the random variable $X \sim N(200, 3600)$.

[2]

- **(b)** Use the model to find $P(150 \le X \le 210)$. [1]
- (c) Use the model to determine x_1 such that $P(160 < X < x_1) = 0.6$, giving your answer correct to five significant figures. [3]

It was found that the smallest and largest masses of the pebbles in this second sample were 112 g and 288 g respectively.

- (d) Use these results to show that the model may not be appropriate. [1]
- (e) Suggest a different value of a parameter of the model in the light of these results. [2]

3. Nov/2020/Paper_H240/02/No.15

In this question you must show detailed reasoning.

The random variable *X* has probability distribution defined as follows.

$$P(X = x) = \begin{cases} \frac{15}{64} \times \frac{2^x}{x!} & x = 2, 3, 4, 5, \\ 0 & \text{otherwise.} \end{cases}$$

(a) Show that
$$P(X=2) = \frac{15}{32}$$
. [1]

The values of three independent observations of X are denoted by X_1 , X_2 and X_3 .

(b) Given that $X_1 + X_2 + X_3 = 9$, determine the probability that at least one of these three values is equal to 2. [6]

Freda chooses values of X at random until she has obtained X = 2 exactly three times. She then stops.

(c) Determine the probability that she chooses exactly 10 values of X. [3]