Continuous Random Variables – 2022 GCE Statistics Further Math A Y542

1. June/2022/Paper_ Y542/01/No.7

The continuous random variable X has probability density function

$$f(x) = \begin{cases} kx^n & 0 \le x \le 1, \\ 0 & \text{otherwise,} \end{cases}$$

where k is a constant and n is a parameter whose value is positive.

It is given that the median of X is 0.8816 correct to 4 decimal places.

Ten independent observations of X are obtained.

Find the expected number of observations that are less than 0.8.

[8]