Impulse and Momentum – 2022 GCE Mechanics Further Math A Y543

1. June/2022/Paper_ Y543/01/No.3

A particle P of mass 6kg moves in a straight line under the action of a single force of magnitude FN which acts in the direction of motion of P.

At time t seconds, where $t \ge 0$, F is given by $F = \frac{1}{5 - 4e^{-t^2}}$.

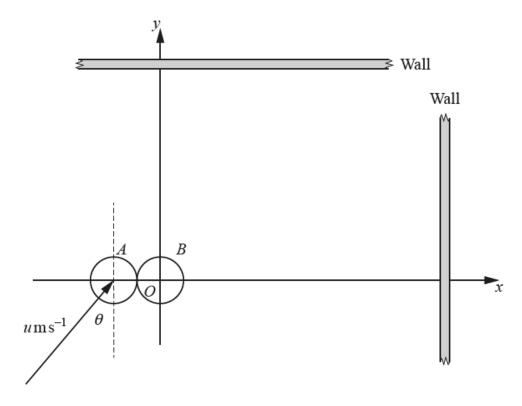
When t = 0, the speed of P is $1.9 \,\mathrm{m\,s^{-1}}$.

- (a) Find the impulse of the force over the period $0 \le t \le 2$. [2]
- (b) Find the speed of P at the instant when t = 2.
- (c) Find the work done by the force on P over the period $0 \le t \le 2$. [2]

2. June/2022/Paper Y543/01/No.8

Two smooth circular discs, A and B, have equal radii and are free to move on a smooth horizontal plane. The masses of A and B are 1 kg and m kg respectively. B is initially placed at rest with its centre at the origin, O. A is projected towards B with a velocity of u m s⁻¹ at an angle of θ to the negative y-axis where $\tan \theta = \frac{5}{2}$. At the instant of collision the line joining their centres lies on the x-axis.

There are two straight vertical walls on the plane. One is perpendicular to the x-axis and the other is perpendicular to the y-axis. The walls are an equal distance from O (see diagram).



After A and B have collided with each other, each of them goes on to collide with a wall. Each then rebounds and they collide again at the same place as their first collision, with disc B again at O.

The coefficient of restitution between A and B is denoted by e. The coefficient of restitution between A and the wall that it collides with is also e while the coefficient of restitution between B and the wall that it collides with is $\frac{5}{9}e$.

It is assumed that any resistance to the motion of A and B may be ignored.

(a) Explain why it must be the case that the collision between A and the wall that it collides with is not inelastic.

(b) Show that
$$e = \frac{1}{m}$$
.

(c) Show that
$$m = \frac{5}{3}$$
. [7]

(d) State one limitation of the model used. [1]