

**Surfaces and Partial Differentiation – 2022 GCE Additional Pure Further Math A Y545****1. June/2022/Paper\_Y545/01/No.1**

The surface  $E$  has equation  $z = \sqrt{500 - 3x^2 - 2y^2}$ .

(a) Determine the values of  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$  at the point  $P$  on  $E$  with coordinates  $(11, -8, 3)$ . [4]

(b) Find the equation of the tangent plane to  $E$  at  $P$ , giving your answer in the form  $ax + by + cz = d$  where  $a, b, c$  and  $d$  are integers. [2]

**2. June/2022/Paper\_Y545/01/No.9**

For all real values of  $x$  and  $y$  the surface  $S$  has equation  $z = 4x^2 + 4xy + y^2 + 6x + 3y + k$ , where  $k$  is a constant and an integer.

(a) Find  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$ . [2]

(b) Determine the smallest value of the integer  $k$  for which the whole of  $S$  lies above the  $x$ - $y$  plane. [7]